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THERMODYNAMIC PROPERTIES OF COMPLEX COPPER CHALCOGENIDES REVIEW

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Abstract: Complex copper-based chalcogenides are a significant environmental-friendly functional material that has great application potential due to their interesting thermoelectric, photoelectric, optical, and other properties, as well as their ionic conductivity. Analysis of numerous studies shows that improving the application characteristics of these compounds is associated with manipulating their structure and composition. An effective solution for optimizing such processes requires their in-depth thermodynamic analysis, which requires reliable data on the fundamental thermodynamic characteristics of the corresponding compounds. This review summarizes the results of researches, including ours works, on the thermodynamic properties of copper chalcogenides with some p¹-p³ elements. The majority of these works were carried out using various modifications of the electromotive force (EMF) method. Planning of experiments carried out by this equilibrium method of chemical thermodynamics and processing of their data is impossible without the presence of reliable data on phase equilibria. Taking this into account, in addition to thermodynamic data, the work also presents the solid-phase equilibria diagrams for a number of systems studied by the EMF method.

The analysis showed that for the Cu-Tl-X, Cu-Ge(Sn)-X (X-S, Se, Te) and Cu-As(Sb, Bi)-S(Se) ternary systems there are mutually consistent data on the phase equilibria and thermodynamic functions of the ternary compounds. For the Cu-Tl-X and Cu-Sn-Se systems, the thermodynamic functions of ternary compounds are obtained by two modifications of the EMF method by determining the partial molar functions of two different components - copper and thallium (tin). The thermodynamic properties of copper chalcogenides with gallium, indium, and silicon have not been extensively researched, and the data that is available is inconsistent.

Keywords: complex copper chalcogenides, ternary copper-containing systems, phase diagrams, thermodynamic properties, EMF method.

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1. Introduction

Binary and complex metal chalcogenides have been widely studied since the middle of the last century as semiconductor, thermoelectric, photoelectric, optical, magnetic, and other functional materials. Many of them have found applications or are considered promising for use in various fields of modern engineering and technology [1-7]. The

development of nanomaterials science and the discovery of new unique quantum states of matter as a topological insulator [8], and then an antiferromagnetic topological insulator [9], gave new impetus to the research of chalcogenides. Studies have shown that many-layered chalcogenides have the properties of a topological insulator [10-14], and some of them

combine the properties of a topological insulator and a magnet [15-17] and are extremely promising for a wide variety of applications in modern high technologies [18-20].

Copper-based chalcogenides occupy an important place among advanced functional materials. In addition to unique electronic properties [3-5, 21-29], they also have high ionic conductivity [30-33] and are considered very promising for use in thermoelectric and photoelectric energy converters and optoelectronic devices, as well as solid-state electrodes and electrolytes, selective membranes, sensors, sensors, etc. Moreover, according to a number of studies in recent years, some copper-based chalcogenides are promising for use in medicine [34, 35]. On the other hand, many copper chalcogenides exist in nature in the form of minerals and are of great interest to the geochemistry of the earth [36, 37].

Analysis of numerous studies on complex copper-containing chalcogenide materials (see Sections 3-5) shows the possibility of significantly improving their functional properties by manipulating the structure and composition. For a better understanding of the relationship between composition, structure and properties, as well as for the search and design of new materials, it is especially important to have reliable, mutually consistent data on the phase equilibria and thermodynamic properties of the corresponding systems [20, 38-40]. The importance of using phase diagrams is that they make it possible not only to identify new compounds or phases of variable composition but also to establish their thermal stability, the nature of formation, areas of primary crystallization and homogeneity, the presence of phase transformations, etc. An effective solution to the optimization of processes requires a deeper thermodynamic analysis, which is only possible if reliable data are available on the fundamental thermodynamic characteristics of the relevant compounds [38].

The purpose of this review is to systematize existing literature data, including the authors' work on the study of the thermodynamic properties of copper chalcogenides with heavy p¹-p³ elements.

Section 2 of the manuscript briefly describes some methodological issues related to

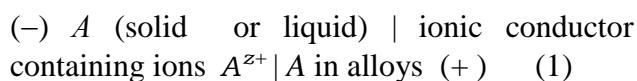
thermodynamic research, especially the electromotive force (EMF) method, which was employed to obtain most thermodynamic data for copper-based chalcogenides. In the following sections, available data on the fundamental thermodynamic characteristics of these ternary compounds and some phases based on them are presented and discussed. Considering the importance of phase diagrams in EMF studies, this manuscript also presents data on solid-phase equilibria of a number of studied systems in addition to thermodynamic data. At the beginning of these sections, a brief overview of works on the most characteristic functional properties of ternary phases of this type is given. The EMF method is employed to obtain thermodynamic data for copper-based chalcogenides.

2. Some methodological issues in the thermodynamic study of metal chalcogenides

An analysis of numerous literature data shows that the EMF method occupies a leading position in the thermodynamic study of metallic and semiconductor, in particular chalcogenide, systems. Various modifications of this method, such as the classical version of concentration cells with a liquid electrolyte, the EMF method with a solid cation- and anion-conducting electrolyte, accelerated modifications of the method, etc. are successfully used in thermodynamic research [41-45].

An important advantage of the EMF method is that it is an equilibrium method of chemical thermodynamics and allows combining thermodynamic research with phase equilibria studies [42, 43]. At the same time, phase equilibria data is important for both experiment planning using the EMF method and processing results.

In practice, thermodynamic studies most often use concentration cells relative to electrodes of the following type [41-43]



where A is the least noble component of the studied system.

EMF measurement data in a certain temperature range are presented in the form of

$$E = a + bT \pm t \left[\frac{S_E^2}{n} + S_b^2(T - \bar{T})^2 \right]^{1/2} \quad (2)$$

recommended in [42]. Here n - is the number of pairs of values E and T ; S_E and S_b are the dispersions of individual EMF measurements and coefficient b , respectively; \bar{T} - the average absolute temperature; t - is Student's criterion.

$$\Delta\bar{G}_A = -zFE \quad (3)$$

$$\Delta\bar{S}_A = zF \left(\frac{\partial E}{\partial T} \right)_p \quad (4)$$

$$\Delta\bar{H}_A = -zF \left[E - T \left(\frac{\partial E}{\partial T} \right)_p \right] \quad (5)$$

the partial molar functions of the mobile component A may be calculated.

Thus, by measuring the equilibrium values of the EMF of concentration cells of type (1) in a wide temperature range for various compositions of the right-hand electrodes, it is possible to calculate the relative partial molar free energy, enthalpy and entropy of component A in a multicomponent solution or heterogeneous mixture.

The issues of organizing and conducting experiments using various variants of the EMF method and methods of mathematical processing of results are discussed in detail in a number of monographs and original works [42-49].

Due to the high accuracy of electrochemical measurements, the determination of thermodynamic functions by the EMF method gives reliable results. The root mean square error of EMF measurements under favorable conditions can be reduced to 0.5 mV, which corresponds to a single determination error of the order of $100 \text{ J}\cdot\text{mol}^{-1}$. This value decreases by another factor of $n^{1/2}$ (n is the number of experimental points) for the average value. Such accuracy is incomprehensible in other methods of thermodynamic study of condensed systems. Relative partial molar entropy and enthalpy, calculated from the temperature coefficient of EMF, are determined with less accuracy. However, experience shows that by ensuring the reversibility of the

linear equations, for example, in the form

$$The Student's criterion is $t \leq 2$ with a confidence level of 95% and the number of experimental points being $n \geq 20$.$$

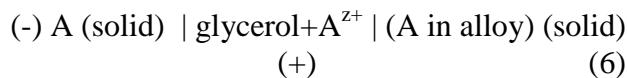
From equations (2) according to the following thermodynamic relations

operation of electrochemical circuits in a wide temperature range, the accuracy of determination of and can reach $0.5 \div 1 \text{ J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$ and $0.3 \div 0.5 \text{ kJ}\cdot\text{mol}^{-1}$, which is comparable with the accuracy of calorimetric measurements [42].

In [42-44], methods for calculating integral thermodynamic functions of ternary and more complex phases based on partial thermodynamic functions of potential-forming components and a phase diagram are described in detail.

Let's consider the main types of concentration cells used in thermodynamic studies of complex chalcogenides.

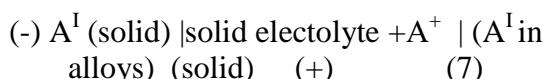
1) In several researches, including studies our group [43, 44, 50-55], concentration cells of the following type



were used in the thermodynamic study of chalcogenide systems.

Using of glycerol solutions of alkali or alkaline earth metals' chlorides makes it possible to conduct experiments in the 300-430 K temperature range, i.e. under conditions close to standard. It should be noted that electrochemical cells with glycerol electrolyte, first applied in 1963 by authors of [56] to amalgam systems, and later successfully used to study various binary and complex systems

2) The discovery of superionic conductors with pure Cu⁺ and Ag⁺ conductivity at room temperature, primarily the Ag₄RbI₅ [57] and Cu₄RbI₃Cl₂ compounds [58], gave new impetus to thermodynamic studies of copper- and silver-containing systems. In a number of works [59-63], concentration cells relative to a copper (silver) electrode with the indicated electrolytes were used to study ternary chalcogenides of copper and silver



(here A^I is Cu⁺ or Ag⁺).

The authors of [64-67] successfully used concentration cells with glassy Ag⁺ conducting electrolyte for thermodynamic studies of silver-containing systems.

It should be noted that to determine the thermodynamic functions of the formation of complex chalcogenide phases, including copper and silver, calorimetric methods are used relatively less frequently. This is apparently due to the complexity of calorimetric experiments, as well as the fact that during the synthesis or combustion of substances in a calorimetric bomb, the processes often do not proceed to completion and it is very difficult to quantify the degree of conversion [38, 43]

At the same time, the differential scanning calorimetry (DSC) is successfully used to determine the thermodynamic functions of reversible phase transitions of the first order - polymorphic transformations or melting [68-70].

3. Copper chalcogenides with elements of the gallium subgroup

Copper chalcogenides with gallium and indium, as well as solid solutions and doped phases based on them, are excellent materials for use in photovoltaic devices [71-84], optoelectronics [75, 85-87], and also as luminescent materials [88- 91].

The use of these phases as solar energy absorbers is due to their band gap, which correlates well with the maximum photon power density in the spectrum of sunlight and at the same time demonstrates long-term stability and

resistance to radiation [82-84]. In the past few years, substantial research has been conducted to enhance their effectiveness. For this purpose, several studies have proposed changing the bulk or surface composition through sulfidization (selenidization) [77, 79, 80], adjusting the ratios of Cu, Ga, and In atoms [73, 84], adding alloying components [71, 78] and other strategies [78]. Note, that by sulfidization of the Cu(Ga, In)Se₂ layers, a solar cell with a record efficiency of 23.35% was obtained [81]. Thin-film solar cells based on Cu(Ga, In)Se₂ are considered as a promising for electricity generation in space stations [82, 84].

Authors of the review [76] using a fundamental thermodynamic approach discussed the main reasons for the relatively low efficiency of photovoltaic systems based on copper-gallium (indium) chalcogenides and ways to optimize methods for obtaining their crystals with specified characteristics. The latest advancements in the production of nanocrystals of these phases with controlled compositions and band gaps are presented in another review [78].

Copper chalcogenide compounds, which have a wide bandgap energy range, are very attractive for applications in optoelectronic and light-emitting devices [86]. Due to their unique optical properties, they can also be used in nonlinear optical devices [87]. The authors of [88] report the development of quantum dot LEDs that exhibit red color with a narrow emission peak by controlling the copper content of Cu-Ga-In-S alloys.

Copper selenides and tellurides with elements of the gallium subgroup, especially thallium, are of interest as thermoelectric materials with low thermal conductivity [92-95].

3.1. The Cu-Ga-X и Cu-In-X (X-S, Se, Te) systems

Copper with gallium and indium forms ternary phases with a wide homogeneity region, which have a disordered cubic structure. With decreasing temperature, these phases transform into low-temperature compounds with ordered structures. The most typical compounds are the CuB^{III}X₂, CuB^{III}₃X₅ and CuB^{III}₅X₈. These compounds form on Cu₂X-B^{III}₂X₃ quasi-binary sections and form stable connodes with the

corresponding elemental chalcogen [96-99].

We have not found any literature data on the thermodynamic properties of copper-gallium

chalcogenides. The thermodynamic properties of copper-indium sulfides and selenides have been studied in a number of works (Table 1).

Table 1. Standard integral thermodynamic functions of ternary compounds of the Cu-Ga(In)-X systems

| Compound | $-\Delta_f G^0(298K)$ | $-\Delta_f H^0(298K)$ | $S^0(298K)$ $J \cdot mol^{-1} \cdot K^{-1}$ | Ref. |
|-----------------------------------|-----------------------|-----------------------|--|-------|
| | $kJ \cdot mol^{-1}$ | | | |
| CuIn ₅ S ₈ | 1238±113 | | | [99] |
| CuInS ₂ | 315±54 | - | | [99] |
| | | 221.8±13 | | [100] |
| | | 327.6 | 136±0.8 [30] | [101] |
| CuIn ₅ Se ₈ | 1060 | | | [102] |
| CuIn ₃ Se ₅ | 380.0±1.4 | 398.2±28.6 | 373±28 | [59] |
| | *467.1±28.0 | *486.3±27.0 | | [59] |
| | 658 | | | [102] |
| CuInSe ₂ | 153.2±0.6 | 158.0±9.6 | 163±11 | [59] |
| | *196.8±9.8 | *201.6±9.2 | | |
| | 220.0 | 218.5 | | [102] |

Note: * - values calculated from data [59] using other thermodynamic data for In₂Te₃.

Table 1 shows that the available data are insufficient and contradictory. Complete complexes of standard integral thermodynamic functions were determined only for compounds CuIn₃Se₅ and CuInSe₂ by the EMF method with a Cu⁺ conducting electrolyte (cell of type 7) [59]. For processing the experimental results, the authors of [54] used the following data for the In₂Se₃ compound: $-\Delta_f G^0(298K) = 224.3 \pm 0.8 \text{ kJ/mol}$; $-\Delta_f H^0(298K) = 239.3 \pm 18.4 \text{ kJ/mol}$; $S_{298}^0 = 201.3 \pm 16.7 \text{ J/(mol}\cdot\text{K)}$. Considering that modern reference books, for example [112], recommend significantly different from the above data ($\Delta_f H^0(298K) = -326.4 \pm 16.7 \text{ kJ/mol}$; $S_{298}^0 = 201.3 \pm 16.7 \text{ J/(mol}\cdot\text{K)}$), the latter was used in our calculations for CuIn₃Se₅ and CuInSe₂ (marked with an asterisk in Table 1). The data obtained for CuInSe₂ are in better agreement with the results of [102].

3.2. The Cu-Tl-X systems

The results of multiple studies on phase equilibria and thermodynamic properties of these systems, carried out before the early 90s of the last century, are summarized in [21].

Below the results of thermodynamic

studies, including more recent studies, as well as brief information of solid-phase equilibria in the appropriate system are given.

The Cu-Tl-S system. The Cu₂S-Tl₂S quasi-binary section of this system was studied almost simultaneously by two teams of authors [103, 104]. According to [103], this system is characterized by the formation of the Cu₉Tl₅, Cu₃Tl₂ and CuTlS ternary compounds. The first two compounds melt with decomposition by peritectic reactions at 706 and 693 K, respectively, and the last one melts congruently at 689 K. According to [104], there are two congruently melting ternary compounds CuTlS and Cu₈Tl₂S₅ in the system. The phase diagram presented in [103] was confirmed by the authors of [105].

The results of a comprehensive study of the phase equilibria of the Cu-Tl-S system are presented in [106-108]. The projection of the liquidus surface, solid-phase equilibria diagram at 300 K and a number of polythermal sections of the phase diagram are constructed. In [108], the results of a thermodynamic study of copper-thallium sulfides by EMF measurements of concentration cells of type (6) are also presented. Later, in [109], a thermodynamic study of the Cu-Tl-S system was carried out by

EMF measurements of concentration cells of type (7) relative to a copper electrode. It should be noted that the thermodynamic data obtained in [108, 109] are independent: they use the results of EMF measurements of different concentration cells, based on which the partial thermodynamic functions of various components of the system - thallium and copper are calculated, which characterize various potential-forming reactions.

Let us consider the results of these works

Table 2. Temperature dependences of the EMF of concentration cells of type (6) in some phase areas of the Cu-Tl-S system ($T=300\div380K$) [108]

| Phase area in Fig.1 | $E, \text{mV} = a + bT \pm 2S_E(T)$ |
|--|---|
| $\text{Cu}_9\text{TlS}_5 + \text{Cu}_2\text{S} + \text{CuS}$ | $580.0 - 0.044T \pm 2\left[\frac{2.4}{40} + 0.0001(T - 346.7)^2\right]^{1/2}$ |
| $\text{Cu}_3\text{TlS}_2 + \text{Cu}_9\text{TlS}_5 + \text{CuS}$ | $585.5 + 0.315T \pm 2\left[\frac{152}{40} + 0.0035(T - 349.6)^2\right]^{1/2}$ |
| $\text{CuTlS} + \text{Cu}_3\text{TlS}_2 + \text{CuTlS}_2$ | $598.6 + 0.351T \pm 2\left[\frac{135}{88} + 0.0017(T - 351.5)^2\right]^{1/2}$ |
| $\text{CuTlS}_2 + \text{CuS} + \text{S}$ | $435.1 + 0.140T \pm 2\left[\frac{40}{57} + 0.0006(T - 350.6)^2\right]^{1/2}$ |

Table 3. Temperature dependences of the EMF of concentration cells of type (7) in some phase areas of the Cu-Tl-S system ($T=300\div380K$) [109]

| Phase area in Fig.1 | $E, \text{mV} = a + bT \pm 2S_E(T)$ |
|--|--|
| $\text{CuTlS}_2 + \text{TlS}_2 + \text{S}$ | $452.2 - 0.056T \pm 2\left[\frac{2.5}{24} + 7.2 \cdot 10^{-5}(T - 343.7)^2\right]^{1/2}$ |
| $\text{CuTlS} + \text{CuTlS}_2 + \text{Tl}_4\text{S}_3$ | $389.4 + 0.086T \pm 2\left[\frac{2.7}{22} + 9.7 \cdot 10^{-5}(T - 346.1)^2\right]^{1/2}$ |
| $\text{Cu}_3\text{TlS}_2 + \text{CuTlS}_2 + \text{CuS}$ | $340.2 + 0.067T \pm 2\left[\frac{1.8}{22} + 5.8 \cdot 10^{-5}(T - 344.1)^2\right]^{1/2}$ |
| $\text{Cu}_9\text{TlS}_5 + \text{Cu}_3\text{TlS}_2 + \text{CuS}$ | $292.1 + 0.134T \pm 2\left[\frac{1.6}{22} + 5.2 \cdot 10^{-5}(T - 342.6)^2\right]^{1/2}$ |

From these equations, using relations (3)-(5), the relative partial thermodynamic functions of

in more detail. In **Fig.1** a solid-phase equilibria diagram of the Cu-Tl-S system is presented. This diagram is characterized by the presence of four ternary compounds, which form a series of three-phase regions between themselves, as well as with binary compounds and the initial components of the system. Tables 2 and 3 list the equations of type (2) for the temperature dependences of the EMF of cells of types (6) and (7).

thallium (Table 4) and copper (Table 5) were calculated.

Table 4. Relative partial thermodynamic functions of thallium in Cu-Tl-S alloys at 298 K

| Phase area in Fig.1 | $-\Delta\bar{G}_{\text{Tl}}$ | $-\Delta\bar{H}_{\text{Tl}}$ | $\Delta\bar{S}_{\text{Tl}}$ $\text{J} \cdot \text{mol}^{-1} \text{K}^{-1}$ |
|--|-----------------------------------|------------------------------|---|
| | $\text{kJ} \cdot \text{mol}^{-1}$ | | |
| $\text{Cu}_9\text{TlS}_5 + \text{Cu}_2\text{S} + \text{CuS}$ | 53.28 ± 0.69 | 44.23 ± 3.99 | 30.36 ± 11.38 |
| $\text{Cu}_3\text{TlS}_2 + \text{Cu}_9\text{TlS}_5 + \text{CuS}$ | 48.56 ± 0.49 | 38.46 ± 2.79 | 33.90 ± 8.07 |
| $\text{CuTlS} + \text{Cu}_3\text{TlS}_2 + \text{CuTlS}_2$ | 46.01 ± 0.30 | 41.98 ± 1.67 | 13.53 ± 4.73 |

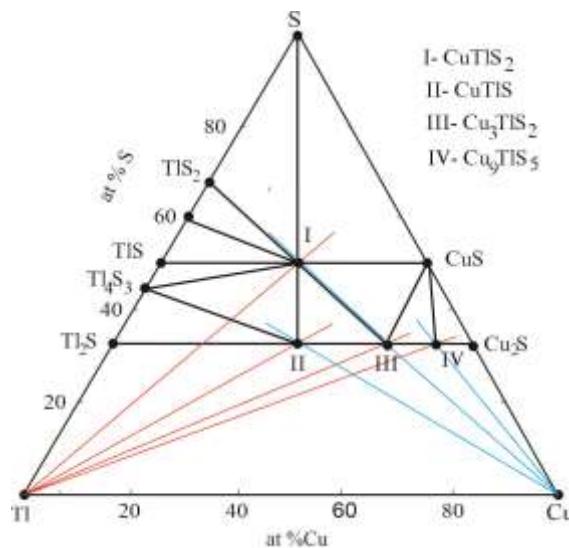
| | | | |
|--|------------------|------------------|------------------|
| $\text{CuTlS}_2 + \text{CuS} + \text{S}$ | 54.69 ± 0.01 | 55.96 ± 0.68 | -4.25 ± 1.93 |
|--|------------------|------------------|------------------|

Table 5. Relative partial thermodynamic functions of copper in Cu-Tl-S alloys at 298 K

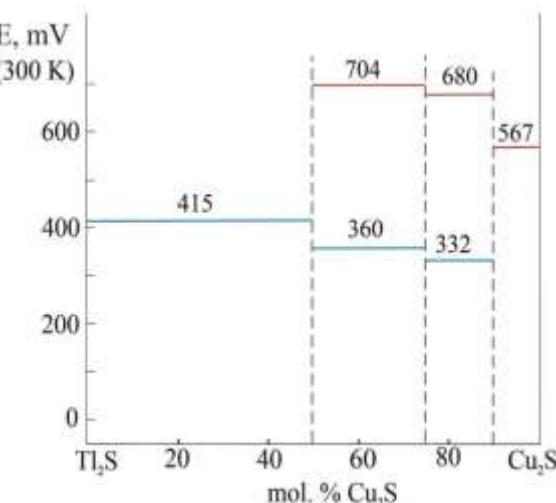
| Phase area in Fig.1 | $-\Delta\bar{G}_{\text{Cu}}$ | $-\Delta\bar{H}_{\text{Cu}}$ | $\Delta\bar{S}_{\text{Cu}}$ |
|--|---------------------------------|--|--|
| | $\text{kJ}\cdot\text{mol}^{-1}$ | $\text{J}\cdot\text{mol}^{-1}\cdot\text{K}^{-1}$ | $\text{J}\cdot\text{mol}^{-1}\cdot\text{K}^{-1}$ |
| $\text{CuTlS}_2 + \text{TlS}_2 + \text{S}$ | 42.02 ± 0.10 | 43.64 ± 0.56 | -5.40 ± 1.64 |
| $\text{CuTlS} + \text{CuTlS}_2 + \text{Tl}_4\text{S}_3$ | 40.04 ± 0.11 | 37.57 ± 0.66 | 8.30 ± 1.90 |
| $\text{Cu}_3\text{TlS}_2 + \text{CuTlS}_2 + \text{CuS}$ | 34.75 ± 0.09 | 32.82 ± 0.52 | 6.46 ± 1.47 |
| $\text{Cu}_9\text{TlS}_5 + \text{Cu}_3\text{TlS}_2 + \text{CuS}$ | 33.20 ± 0.08 | 28.18 ± 0.50 | 12.93 ± 1.38 |

The EMF isotherms of cells (6) and (7) along the $\text{Cu}_2\text{S}-\text{Tl}_2\text{S}$ section are presented in Fig.2. As can you see, the EMF values of both types of cells is constant within a certain phase region and changes abruptly when moving from one phase region to another. In this case, the numerical values of the EMF increase with a decrease in the thallium concentration in the alloys. For cells (6) this is expected, but for cells (7) such a picture, at first view, contradicts the well-known requirement [43] that it is

impossible to reduce the EMF value with a decrease in the concentration of the potential-forming component in the alloy. However, a comparison of Fig. 2 with the phase diagram (Fig. 1) shows that both dependences are in accordance with the above requirement, namely, the EMF values increase with decreasing concentration of the potential-forming component along the corresponding ray straight lines (red and blue lines in Fig. 1).

**Fig.1.** The solid-phase equilibria diagram of the Cu-Tl-S system at 300 K.

The partial molar functions of thallium and copper (Tables 4 and 5) characterize various virtual potential formation reactions. According to the phase diagram (Fig. 1), the partial molar

**Fig.2.** EMF isotherms of concentration cells (6) and (7) along the $\text{Cu}_2\text{S}-\text{Tl}_2\text{S}$ section

values of thallium in the indicated phase regions (Table 4) are the thermodynamic characteristics of the following potential formation reactions (all substances are in crystalline form):





Similarly, the partial molar functions of copper (Table 5) are the thermodynamic characteristics



Using the above equations for potential formation reactions, the standard thermodynamic functions of formation and standard entropies of copper-thallium sulfides

$$\Delta Z_{\text{CuTiS}_2}^0 = \Delta \bar{Z}_{\text{Tl}} + \Delta Z_{\text{CuS}}^0 \quad (16)$$

$$S_{\text{CuTiS}_2}^0 = \Delta \bar{S}_{\text{Tl}} + S_{\text{Tl}}^0 + S_{\text{CuS}}^0 \quad (17)$$

(here $\Delta Z^0 \equiv \Delta G^0$ or ΔH^0 of the corresponding compound, $\Delta \bar{Z} \equiv \Delta \bar{G}_{\text{Cu}}$ or $\Delta \bar{H}_{\text{Cu}}$) and taking

$$\Delta Z_{\text{CuTiS}_2}^0 = \Delta \bar{Z}_{\text{Cu}} + \Delta Z_{\text{TiS}_2}^0 \quad (18)$$

$$S_{\text{CuTiS}_2}^0 = \Delta \bar{S}_{\text{Cu}} + S_{\text{Cu}}^0 + S_{\text{TiS}_2}^0 \quad (19)$$

In addition to the partial molar values of thallium or copper (Tables 4 and 5), thermodynamic data for the compounds TiS_2 , Ti_4S_3 [110], Cu_2S and CuS [111] (Table 6), as well as standard entropies of copper ($S_{298}^0 = 33.1 \pm 0.5 \text{ J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$) and thallium (S_{298}^0

of the below potential formation reactions:

were calculated. For example, in accordance with reaction (8) for the CuTiS_2 compound, calculations were carried out using the relations

into account reaction (12) according to the relations:

$= 64.18 \pm 0.21 \text{ J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$ [112] were used for calculations equations (8)-(15).

The obtained two series of values of standard integral thermodynamic functions of copper-thallium sulfides are listed in Table 6.

Table 6. Standard integral thermodynamic functions of ternary compounds of the Cu-Tl-S system and some binary compounds used in calculations

| Compounds | $-\Delta_f G^0(298\text{K})$ | $-\Delta_f H^0(298\text{K})$ | $S^0(298\text{K})$ $\text{J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$ | Ref. |
|---------------------------|-----------------------------------|------------------------------|--|-------|
| | $\text{kJ} \cdot \text{mol}^{-1}$ | | | |
| CuS | 36.8 ± 0.4 | 42.7 ± 3.4 | 46.4 ± 2.9 | [111] |
| Cu_2S | 66.1 ± 0.8 | 63.2 ± 5.9 | 108.8 ± 5.4 | [111] |
| TiS_2 | 52.3 ± 0.5 | 50.0 ± 0.8 | 145.0 ± 0.9 | [110] |
| Ti_4S_3 | 196.8 ± 1.5 | 197.4 ± 6.5 | 348.5 ± 20.5 | [110] |
| CuTiS_2 | 91.5 ± 0.5 | 98.6 ± 4.0 | 172.7 ± 2.8 | [108] |
| | 94.3 ± 0.7 | 93.6 ± 1.4 | | [109] |
| CuTiS | 84.1 ± 1.5 | 82.1 ± 4.9 | 132.4 ± 6.2 | [108] |
| | 90.3 ± 0.7 | 88.3 ± 2.1 | | [109] |
| Cu_3TiS_2 | 152.7 ± 1.8 | 145.8 ± 12.3 | | [108] |

| | | | | |
|---------------------------|-----------|------------|------------|-------|
| | 163.8±2.6 | 159.2±9.8 | 251.8±5.8 | [109] |
| Cu_9TlS_5 | 354.6±4.5 | 339.7±30.8 | | [108] |
| | 373.8±3.9 | 371.8±21.4 | 529.0±19.0 | [109] |

Table 6 shows that the values of the standard thermodynamic functions for the formation of ternary compounds obtained by two modifications of the EMF method are in satisfactory agreement with each other. This confirms the reversibility of the concentration cells of (6) and (7) types, and the reliability of thermodynamic data for copper and thallium sulfides [110,111], used by the authors [108, 109] in the calculations.

The Cu-Tl-Se system. The quasi-binary $\text{Cu}_2\text{Se}-\text{Tl}_2\text{Se}$ section of this system is characterized by the formation of the ternary CuTlSe , $\text{Cu}_7\text{Tl}_3\text{Se}_5$, Cu_3TlSe_2 , $\text{Cu}_8\text{Tl}_2\text{Se}_5$ and Cu_9TlSe_5 compounds [113]. According to [21], the $\text{CuTlSe}-\text{TlSe}$, $\text{CuTlSe}-\text{Tl}$ and $\text{CuTlSe}-\text{Se}$ sections are also quasi-binary. The first section forms a phase diagram of a simple eutectic type,

the second section is related to a monotectic type, and the third one is characterized by the formation of an incongruently melting ternary CuTlSe_2 compound.

There is literature data about the synthesis and crystal structure of ten copper selenides with thallium [21, 114]. However, up to now, a complete picture of phase equilibria in the Cu-Tl-Se system has not been obtained. In [115], a fragment of the solid-phase equilibria diagram of this system was constructed, which reflected three ternary compounds (Fig. 3) and their thermodynamic properties were studied by the EMF method with a solid electrolyte. For the compounds CuTlSe_2 and CuTlSe , the corresponding thermodynamic data were previously obtained [43] by EMF measurements of (6) type cells (Table 7).

Table 7. Standard thermodynamic functions of formation and standard entropies of TlSe and some ternary phases of the Cu-Tl-Se and Cu-Tl-Te systems

| Compounds | $-\Delta_f G^0(298\text{K})$ | $-\Delta_f H^0(298\text{K})$ | $S^0(298\text{K}), \text{J}\cdot\text{mol}^{-1}\cdot\text{K}^{-1}$ | Ref |
|---|---------------------------------|------------------------------|--|----------------|
| | $\text{kJ}\cdot\text{mol}^{-1}$ | | | |
| CuTlSe_2 | 96.29±0.16 | 97.91±0.95 | 176.1±5.1 | [115] [43] |
| | 96.5±0.6 | 97.2±1.3 | | |
| CuTlSe | 84.49±0.16 | 81.37±0.85 | 149.9±2.8 | [115] [43] |
| | 84.2±1.3 | 80.5±3.9 | | |
| Cu_2TlSe_2 | 119.06±0.27 | 118.61±1.54 | 216.2±6.8 | [115] |
| CuTlTe_2 | 75.1±0.4 | 72.6±1.3 | 208±4 | [118] |
| Cu_2TlTe_2 | 99.2±0.5 | 94.3±2.1 | 249±6 | [118] [119] |
| | 94.8±0.9 | 92±7 | 237±3 | |
| Cu_3TlTe_2 | 122.0±0.6 | 115.2±2.7 | 288±8 | [118] [119] |
| | 117.1±1.2 | 117±5 | 263±4 | |
| Cu_9TlTe_5 | 264.3±2.6 | 253.8±9.8 | 637±15 | [118] [119] |
| | 244.0±2.4 | 2431±14 | 621±7 | |
| $\delta(\text{Cu}_{0.2}\text{Tl}_{4.8}\text{Te}_3)$ | 210.2±1.7 | 213.0±2.2 | 454±7 | [118] |
| $\delta(\text{Cu}_{0.4}\text{Tl}_{4.6}\text{Te}_3)$ | 207.8±1.6 | 210.5±2.3 | 449±7 | [118] |
| $\delta(\text{Cu}_{0.6}\text{Tl}_{4.4}\text{Te}_3)$ | 205.3±1.6 | 207.6±2.4 | 444±8 | [118] |
| $\delta(\text{Cu}_{0.8}\text{Tl}_{4.2}\text{Te}_3)$ | 203.8±1.5 | 206.0±2.5 | 438±8 | [118] |
| CuTl_4Te_3 | 201.4±1.4 | 203.8±2.6 | 433±9 | [118] |

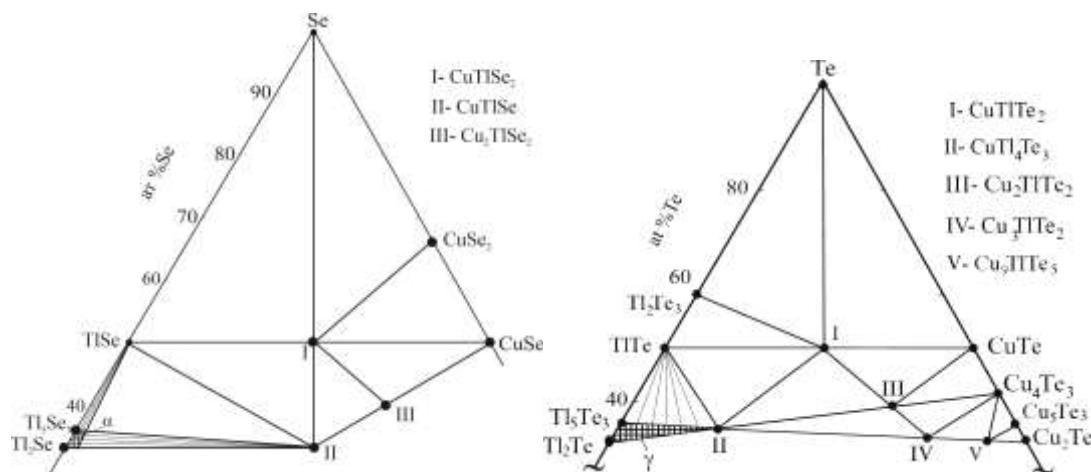


Fig. 3. Fragments of solid-phase equilibria diagrams of the Cu-Tl-Se [115] and Cu-Tl-Te [118] systems at 300 K.

The Cu-Tl-Te system. According to available data [21, 118], the Cu₂Te-Tl₂Te section is non-quasi-binary and is characterized by the formation of ternary Cu₉TlTe₅ and Cu₃TlTe₂ compounds with incongruent melting. Ternary compounds with the compositions CuTlTe₂, Cu₂TlTe₂ and CuTl₄Te₃ are also reported [21, 114, 116, 117].

The fragments of the Cu-Tl-Te solid-phase equilibria diagram and the results of a thermodynamic study of some copper-thallium tellurides by EMF measurements of concentration cells (6) and (7) are presented by authors of [118, 119]. Figure 3 shows the phase diagram at 300 K according to the data of [119], which reflects the above ternary compounds. The integral thermodynamic functions of three of them were determined by two modifications of the EMF method and are in satisfactory agreement (the discrepancies do not exceed 10%). Table 7 also shows thermodynamic data for CuTl₄Te₃-Tl₅Te₃ solid solutions [118].

4. Copper chalcogenides with p² elements

The most characteristic and studied copper chalcogenides with p²-elements are compounds of the Cu₂B^{IV}X₃ and Cu₈B^{IV}X₆ types. Below is a brief overview of studies on the functional properties of these compounds.

Compounds of the Cu₂B^{IV}X₃ type, especially Cu₂SnSe₃, Cu₂GeSe₃, and alloys based on them have been widely studied as environmentally friendly and affordable thermoelectric materials [120-130]. It has been

shown that Cu₂SnSe₃ doped with various elements (In, Zn, Ag, Sb, Pb, S, Te) [123, 124, 126, 129], as well as its composites with graphene and other phases [125, 128, 130], demonstrate good thermoelectric indicators. The thermoelectric characteristics of Cu₂GeSe₃ doped with various elements [121, 129], as well as solid solutions based on it [122] also improve.

Studies have shown that Cu₂B^{IV}X₃ compounds are also promising for use as photovoltaic and optoelectronic materials [131-144]. The photoelectric and optical properties of the Cu₂SnS₃ compound and alloys based on it have been studied in most detail [136-144]. Authors of [134] presents a review of works on the synthesis, structural transformation, morphological engineering and restructuring of the energy gap of nanoparticles of Cu-Sn-S(Se) systems and discusses the prospects for the development of solar cells based on them. In addition, other photovoltaic applications such as photoelectrocatalytic hydrogen production and dye degradation of Cu-Sn-S(Se) nanoparticles are also noted.

Another review [144] shows that the Cu₂SnS₃ ternary compound, consisting of non-toxic and readily available elements, is the preferred photovoltaic material for solar cell applications due to its optimal structural and optical properties. This paper also discusses the issues of efficiency loss in solar cells based on this compound and possible ways to eliminate them.

Copper-containing compounds of the

argyrodite family with the general formula $\text{Cu}_8\text{B}^{\text{IV}}\text{X}_6$ are also of great interest as effective ionic conductors, thermoelectric, photoelectric and nonlinear optical materials [145].

Cu argyrodites, being typical superionic semiconductors with two independent structural units (a rigid anionic framework and weakly bound Cu^+ cations), can serve as very good base compounds for the development of high-performance thermoelectric materials by separately tuning the electrical and thermal properties [145, 146]. It should be noted that only a small part of the research of the thermoelectric properties of argyrodites is devoted to the study of compounds of stoichiometric composition [146-148]. Most of the existing works on argyrodite thermoelectrics are focused on the production of nano- and single crystals, thin films, high-density polycrystals, complex phases, and composite materials based on them [145, 146, 149-151]. To increase thermoelectric efficiency, researchers often vary the composition of argyrodite compounds in the following ways [145]: 1. Complicating the composition through various types of substitution with analogue atoms; 2. Adding dopants; 3. Creation of a deficiency of individual elements in the stoichiometric composition.

The optical properties of some $\text{A}^{\text{I}}\text{B}^{\text{IV}}\text{X}_6$ compounds were studied in [152, 153]. It was shown [152] that replacing Ag with Cu in isostructural $\text{A}^{\text{I}}\text{B}^{\text{IV}}\text{X}_6$ compounds causes a clear increase in secondary harmonic generation. This result opens up the possibility of synthesizing high-quality infrared nonlinear optical materials based on them. Authors of [153] report the preparation of Cu_8SiS_6 and Cu_8SiSe_6 thin-film layers for optoelectronic applications.

4.1. The Cu-Si-X systems

Phase equilibria in the Cu-Si-S-Se ternary systems were studied along quasi-binary $\text{Cu}_2\text{S}-\text{SiS}_2$ [154] and $\text{Cu}_2\text{Se}-\text{SiSe}_2$ sections [155]. According to these works, copper and silicon form ternary compounds of the Cu_8SiX_6 and Cu_2SiX_3 compositions. The thermodynamic properties of these compounds have been practically not studied. There are works [68-70] in which the functions of phase transitions of some compounds were determined by the DSC method. These data are given in subsection 4.2.

(Table 10).

4.2. The Cu-Ge-X systems

The Cu-Ge-S system. According to [156, 157], the $\text{Cu}_2\text{S}-\text{GeS}_2$ quasi-binary section is characterized by the formation of Cu_8GeS_6 and Cu_2GeS_3 compounds with incongruent melting at 1253 and 1213 K. Cu_8GeS_6 undergoes a polymorphic transformation at 328 K. An isothermal section of the phase diagram of the Cu-Ge-S system at 300 K (Fig. 4), at which the above ternary compounds were reflected is presented in [21].

The Cu-Ge-Se system. According to [158], the nature of phase equilibria along the $\text{Cu}_2\text{Se}-\text{GeSe}_2$ section is similar to the sulfide system: ternary compounds Cu_8GeSe_6 and Cu_2GeSe_3 melt with decomposition by peritectic reactions at 1080 K and 1037 K. The presented in [159] T-x diagram confirms Cu_2GeSe_3 compound with congruent melting at 1033 K, but instead of Cu_8GeSe_6 a compound of similar composition Cu_6GeSe_5 is presented. Later, this system was re-studied in the composition range of 15-60 mol% GeSe_2 [160] and it was shown that the congruent melting temperature of Cu_2GeSe_3 is 1053 K, and Cu_8GeSe_6 melts with decomposition at 1083 K and has a polymorphic transformation at 328 K.

The Cu-Ge-Te system studied in a number of works, the results of which are summarized in [21]. There is one ternary compound Cu_2GeTe_3 in the system.

Fig. 4 shows the phase diagrams of the Cu-Ge-S, Cu-Ge-Se and Cu-Ge-Te systems at room temperature [21]. The thermodynamic properties of copper-germanium chalcogenides were studied in [45, 161-163, 167] by EMF measurements of concentration cells of type (7).

When planning experiments on the Cu-Ge-S and Cu-Ge-Se systems, the authors of [161] proceeded from the fact that the Cu_8GeS_6 and Cu_8GeSe_6 compounds have polymorphic transitions in the temperature range of EMF measurements. Experiments have shown that the temperature dependences of the EMF for electrode alloys containing the Cu_8GeS_6 and Cu_8GeSe_6 compounds have the form of two straight lines with a break point at the temperature of their polymorphic transformation (Fig. 5). From the EMF measurements data, the partial molar functions of copper were

calculated for two modifications of the indicated compounds (Table 8), which were used to calculate the thermodynamic functions of

formation (Table 9) and polymorphic transitions (Table 10).

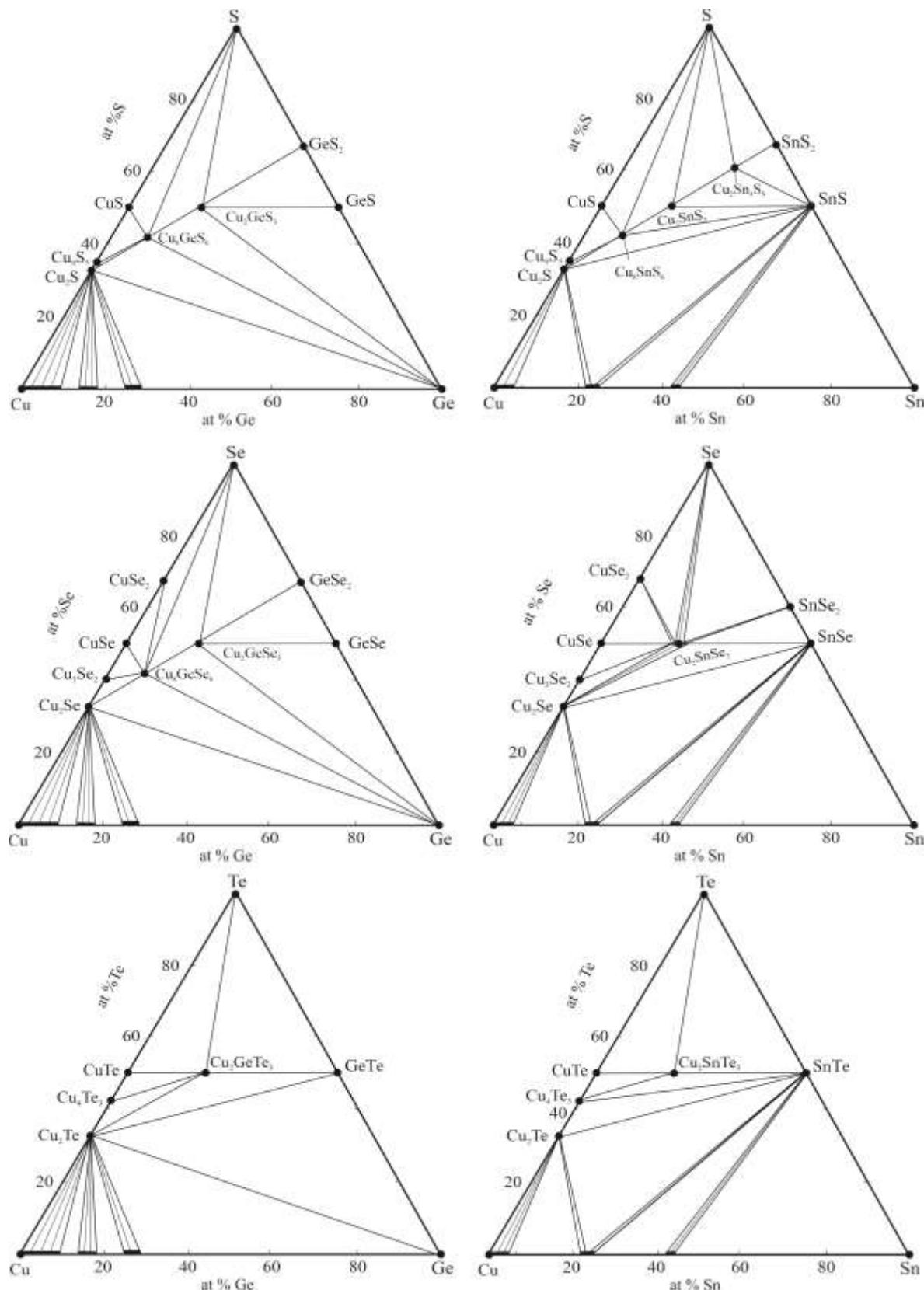


Fig.4. Solid-phase equilibria diagrams of Cu-Ge-X and Cu-Sn-X systems at 300 K [21].

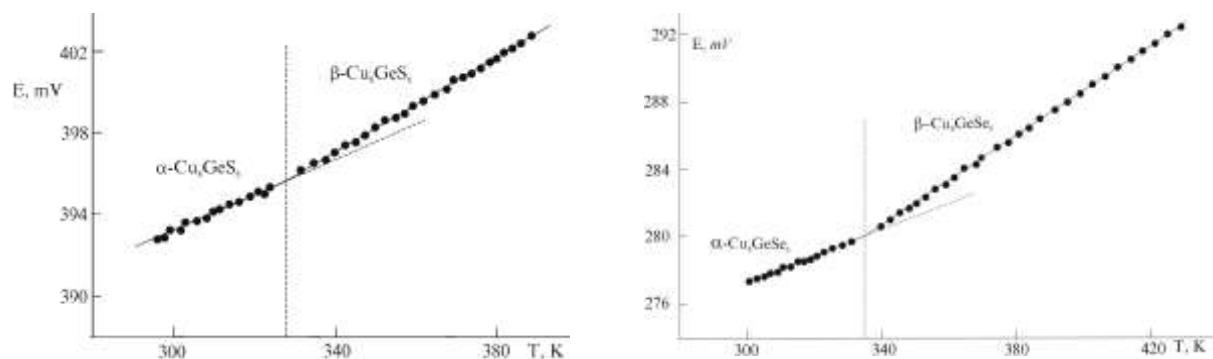


Fig.5. EMF dependences of concentration cells (7) for Cu_8GeS_6 and Cu_8GeSe_6 compounds [161]

Table 8. Partial molar thermodynamic functions of copper in some phase regions of the Cu-Ge-S and Cu-Ge-Se systems [161]

| Phase area | T, K | $-\bar{\Delta}G_{\text{Cu}}$ | $-\bar{\Delta}H_{\text{Cu}}$ | $\Delta\bar{S}_{\text{Cu}}$ $\text{J}\cdot\text{mol}^{-1}\cdot\text{K}^{-1}$ |
|--|------|---------------------------------|---------------------------------|---|
| | | $\text{kJ}\cdot\text{mol}^{-1}$ | $\text{kJ}\cdot\text{mol}^{-1}$ | |
| $\alpha\text{-Cu}_8\text{GeS}_6+\text{Cu}_2\text{GeS}_3+\text{S}$ | 298 | 37.925 ± 0.013 | 35.37 ± 0.32 | 8.56 ± 1.04 |
| $\beta\text{-Cu}_8\text{GeS}_6+\text{Cu}_2\text{GeS}_3+\text{S}$ | 400 | -39.000 ± 0.098 | 34.52 ± 0.55 | 11.19 ± 1.52 |
| $\alpha\text{-Cu}_8\text{GeSe}_6+\text{Cu}_2\text{GeSe}_3+\text{Se}$ | 298 | 26.735 ± 0.009 | 24.59 ± 0.19 | 7.20 ± 0.59 |
| $\beta\text{-Cu}_8\text{GeSe}_6+\text{Cu}_2\text{GeSe}_3+\text{Se}$ | 400 | 27.856 ± 0.059 | 22.61 ± 0.27 | 13.12 ± 0.70 |

Table 9. Standard integral thermodynamic functions of the argyrodite family compounds

| Phase | $-\Delta_f G^0$ | $-\Delta_f H^0$ | S^0 $\text{J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$ | Ref. |
|------------------------------------|---------------------------------|---------------------------------|---|-----------|
| | $\text{kJ}\cdot\text{mol}^{-1}$ | $\text{kJ}\cdot\text{mol}^{-1}$ | | |
| Cu_2GeS_3 | 211.3 ± 2.4 | 213.7 ± 2.3 | 190.3 ± 5.5 | [167] |
| $\text{RT-Cu}_8\text{GeS}_6$ | 438.9 ± 2.5 | 425.9 ± 4.2 | 536.3 ± 13.1 | [161] |
| $\text{HT-Cu}_8\text{GeS}_6$ | $*445.3\pm 3.1$ | 420.8 ± 5.6 | 552.1 ± 15.8 | [161] |
| Cu_2GeSe_3 | 178.4 ± 18.8 | 174.5 ± 19.7 | 223.4 ± 6.6 | [45] |
| | 176.8 ± 3.1 | 173.9 ± 3.1 | 233.3 ± 5.1 | [162] |
| $\text{RT- Cu}_8\text{GeSe}_6$ | 341.1 ± 3.3 | 327.4 ± 4.5 | 596.7 ± 11.6 | [161] |
| | 105.1 ± 1.9 | 114.5 ± 9.2 | 143 ± 2 | [162] |
| $\text{HT- Cu}_8\text{GeSe}_6$ | $*348.1\pm 3.7$ | 315.6 ± 5.0 | 632.3 ± 12.5 | [161] |
| $\text{Cu}_2\text{Sn}_4\text{S}_9$ | 659.9 ± 4.3 | 650.9 ± 29.7 | 560.3 ± 74.7 | [45] |
| | 165.4 ± 1.5 | 141.6 ± 6.3 | 639.8 ± 18.3 | [165] |
| Cu_2SnS_3 | 239.6 ± 1.5 | 242.6 ± 12.0 | 196.3 ± 21.9 | [45] |
| | 169.3 ± 1.3 | 150.0 ± 5.5 | 278.6 ± 15.7 | [165] |
| Cu_4SnS_4 | 316.4 ± 2.4 | 327.7 ± 18.8 | 266.5 ± 28.2 | [45] |
| | 261.3 ± 2.4 | 220.8 ± 9.4 | 414.4 ± 20 | [165] |
| Cu_2SnSe_3 | 189.5 ± 2.6 | 187.5 ± 4.8 | 251.6 ± 5.0 | [45, 166] |
| | 198.4 ± 0.6 | 198.5 ± 2.9 | 237 ± 5 | [43] |
| Cu_2SnTe_3 | 117.7 ± 1.4 | 116.2 ± 2.4 | 264 ± 6 | [45] |

*Note: data at 400 K is marked with an asterisk.

In [161], the thermodynamic functions of the polymorphic transformations of the Cu_8GeS_6 and Cu_8GeSe_6 compounds were calculated from EMF measurements data. Let us consider the

method of these calculations using Cu_8GeS_6 as an example. Since in the temperature range of EMF measurements the heat of formation of this compound is almost constant, then

$$\Delta H_{p.t.} = \Delta_f H^0(\beta) - \Delta_f H^0(\alpha) . \quad (20)$$

where $\Delta H_{p.t.}$ - is the heat of polymorphic transformation; $\Delta_f H^0(\beta)$ and $\Delta_f H^0(\alpha)$ - are the



it follows that the contribution of Cu_2GeS_3 to the $\Delta_f H^0(\beta)$ and $\Delta_f H^0(\alpha)$ functions is the same.

$$\Delta H_{p.t.} = 6[\bar{\Delta H}_{\text{Cu}}(\beta) - \bar{\Delta H}_{\text{Cu}}(\alpha)].$$

which does not include the value and error of the heat of formation of Cu_2GeS_3 .

$$\Delta S_{p.t.} = \Delta H_{p.t.} / T_{p.t.}$$

Table 10 shows the thermodynamic functions of phase transitions of these compounds and their silicon analogues, obtained by the DSC method [69, 70, 164]. Table 10 demonstrates that the data obtained by both methods (exception for the Cu_8GeS_6) are in

heats of formation of two modifications of this compound. On the other hand, from following relation

$$(21)$$

Therefore, the calculation of $\Delta H_{p.t.}$ was carried out according to the relation

$$(22)$$

The entropy of the polymorphic transformation is calculated using the relation

$$(23)$$

good agreement. Calorimetric data is more accurate. Relatively high errors in the data obtained by the EMF method are due to the fact that in this method partial enthalpy and entropy are calculated indirectly from the temperature dependence coefficient of the EMF [42, 43].

Table 10. Temperatures and thermodynamic functions of phase transitions of some $\text{Cu}_8\text{B}^{IV}\text{X}_6$ compounds

| Compound | T _{p.t.} | $\Delta H_{p.t.}$, kJ·mol ⁻¹ | $\Delta S_{p.t.}$, J·mol ⁻¹ ·K ⁻¹ | Method, Ref. |
|----------------------------|-------------------|--|--|--------------|
| Cu_8GeS_6 | 328 | 5.1±2.4 | 15.5±7.5 | EMF, [161] |
| | 330 | 15.54±0.62 | 47.09±1.88 | DSC, [70] |
| Cu_8GeSe_6 | 335 | 11.9±2.8 | 35.5±8.4 | EMF, [161] |
| | 330 | 11.23±0.45 | 34.03±1.36 | DSC, [164] |
| Cu_8SiS_6 | 336 | 14.85±0.59 | 44.20±1.77 | DSC, [70] |
| Cu_8SiSe_6 | 325 | 14.73±0.59 | 45.32±1.81 | DSC,[69] |

4.3. The Cu-Sn-X systems

The Cu-Sn-S system. Some polythermal sections of this system were studied in the 70s of the last century and summarized in [21]. It is shown that the $\text{Cu}_2\text{S}-\text{SnS}$ and $\text{Cu}_2\text{S}-\text{SnS}_2$ sections are quasi-binary. The first belongs to the eutectic type, and in the second 4 intermediate phases are formed: Cu_2SnS_3 , Cu_4SnS_4 , $\text{Cu}_4\text{Sn}_3\text{S}_6$, and $\text{Cu}_2\text{Sn}_4\text{S}_9$. The isothermal section of the phase diagram at 300 K (Fig. 4), presented in [21], reflects the above copper-tin sulfides.

The Cu-Sn-Se system. The only ternary compound of this system, Cu_2SnSe_3 , is formed

on the quasi-binary $\text{Cu}_2\text{Se}-\text{SnSe}_2$ section and melts congruently at 963 K [21]. The T-x-y diagram and isothermal section of the phase diagram at 300 K (Fig. 4) based on data from a number of works were constructed in [21].

The Cu-Sn-Te system. In [21], a complete T-x-y diagram of this system is presented, characterized by the presence of one ternary compound Cu_2SnTe_3 . This compound has a cubic structure and melts incongruently at 680 K.

The thermodynamic properties of copper-tin chalcogenides were studied by the EMF method with a solid electrolyte [45, 165, 166],

and the Cu_2SnSe_3 compound was also studied by the classical version of the EMF method with a liquid electrolyte. From the measurement data of the EMF of cells of type (7) using relations (3)-(5), the partial molar functions of copper in the alloys were calculated. The authors employed solid-phase equilibrium diagrams of the corresponding systems (Fig. 4) to calculate the integral thermodynamic functions. Table 9 show that the thermodynamic functions of Cu_2SnSe_3 obtained by two modifications of the EMF method are in good agreement with each other. It is also clear from Table 9 that the numerical values of the thermodynamic functions of copper-tin sulfides according to [165] are significantly lower than the data from [45]. For the compounds $\text{Cu}_2\text{Sn}_4\text{S}_9$ and Cu_4SnS_4 , the data [165] are even lower than the

sum of the corresponding values for Cu_2S and SnS_2 , which is thermodynamically impossible. It was noted in [21] that this is the result of incorrect definition of potential-forming reactions by the authors of [165].

4.4. Quaternary systems including chalcogenides of copper and p²-elements

In the last decade, in order to search for solid solutions with various types of substitutions based on copper chalcogenides with p² elements, some quasi-ternary ($\text{Cu}_2\text{S}-\text{Ag}_2\text{S}-\text{GeS}_2$ [168], $\text{Cu}_2\text{Se}-\text{Ag}_2\text{Se}-\text{GeSe}_2$ [168], $\text{Cu}_2\text{Se}-\text{GeSe}_2-\text{SnSe}_2$ [169], $\text{Cu}_2\text{S}-\text{Cu}_8\text{SiS}_6-\text{Cu}_8\text{GeS}_6$ [70], $\text{Cu}_2\text{Se}-\text{Cu}_8\text{SiSe}_6-\text{Cu}_8\text{GeSe}_6$ [170]) and reciprocal ($2\text{Cu}_2\text{S}+\text{GeSe}_2 \leftrightarrow 2\text{Cu}_2\text{Se}+\text{GeS}_2$ [171, 172], $2\text{Cu}_2\text{S}+\text{SnSe}_2 \leftrightarrow 2\text{Cu}_2\text{Se}+\text{SnS}_2$ [168]) systems.

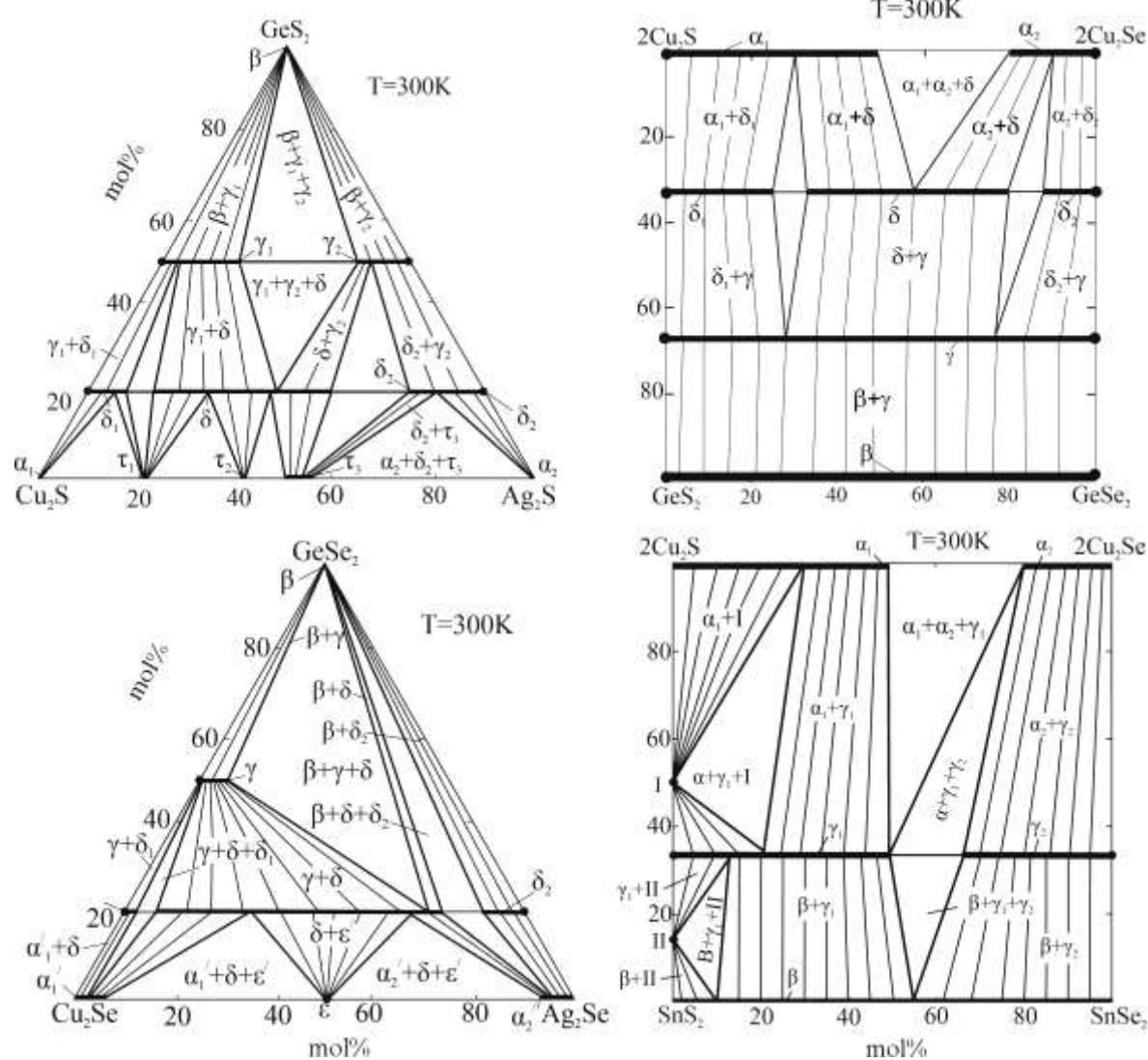


Fig.6. Solid-phase equilibria diagrams of quasi-ternary $\text{Cu}_2\text{S}-\text{Ag}_2\text{S}-\text{GeS}_2$ $\text{Cu}_2\text{Se}-\text{Ag}_2\text{Se}-\text{GeSe}_2$ and reciprocal $2\text{Cu}_2\text{S}+\text{GeSe}_2 \leftrightarrow 2\text{Cu}_2\text{Se}+\text{GeS}_2$ и $2\text{Cu}_2\text{S}+\text{SnSe}_2 \leftrightarrow 2\text{Cu}_2\text{Se}+\text{SnS}_2$ systems

Isothermal sections of phase diagrams at room temperature (Fig. 6) clearly demonstrate the formation of unlimited or broad solid solutions based on ternary compounds. A number of works [70, 167-169, 172-175] present the results of a comprehensive study of phase equilibria and thermodynamic properties of the above and some similar systems.

As an example, let's consider Cu₂S-Ag₂S-GeS₂ system [167]. The results of EMF measurements of concentration chains of type (7) were in accordance with the solid-phase equilibrium diagram (Fig. 6) and confirmed the formation of wide areas of solid solutions based

on Cu₂GeS₃ and Ag₂GeS₃ compounds. The concentration dependence curves of EMF (Fig. 7) and partial molar functions of copper at 298 K (Fig. 8) have a form which is characteristic for systems with the formation of limited solid solutions based on the starting compounds. Within the homogeneity region of α- and β-solid solutions based on Cu₂GeS₃ and Ag₂GeS₃, respectively, the partial molar functions of copper are monotonic functions of composition, and in the heterogeneous α+β region have constant values, since the compositions of the coexisting phases are almost constant.

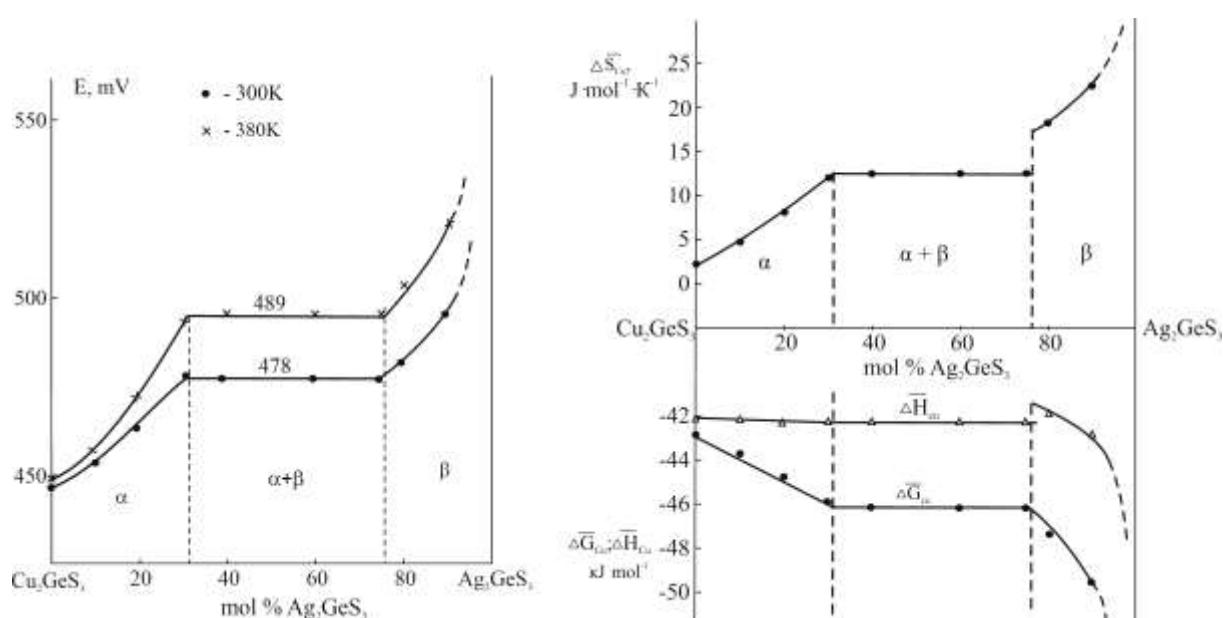


Fig.7. Isotherms of EMF of cells of type (7) and partial molar functions of copper in the Cu₂GeS₃-Ag₂GeS₃ system

Based on the analysis of the Cu-Ag-Ge-S concentration tetrahedron (Fig. 8), the authors of [167] determined potential-forming reactions for individual compositions of Cu_{2-x}Ag_xGeS₃ solid solutions. As can be seen, the ray lines from the top of Cu, passing through the Cu₂GeS₃-Ag₂GeS₃ section, reach the concentration plane of the side ternary system

Ag-Ge-S in the three-phase region Ag₂GeS₃+GeS₂+S. Therefore, in the overall potential-forming reaction for Cu_{2-x}Ag_xGeS₃ solid solutions, the phases of the indicated three-phase region and elemental copper must interact. For example, for a solid solution with Cu_{0.2}Ag_{1.8}GeS₃ composition the potential-forming reaction has following form:



and the relations for calculating its integral thermodynamic functions ($\Delta Z \equiv \Delta G$ or ΔH) as

$$\begin{aligned}\Delta_f Z^0 &= 0.2\bar{\Delta}Z_{\text{Cu}} + 0.9\bar{\Delta}Z^0(\text{Ag}_2\text{GeS}_3) + 0.1\bar{\Delta}f Z^0(\text{GeS}_2) \\ S^0 &= 0.2\bar{\Delta}S_{\text{Cu}} + 0.2S^0(\text{Cu}) + 0.9S^0(\text{Ag}_2\text{GeS}_3) + 0.1S^0(\text{GeS}_2) + 0.1S^0(\text{S})\end{aligned}$$

In a similar way, the standard integral thermodynamic functions of $\text{Cu}_{2-x}\text{Ag}_x\text{GeS}_3$ solid solutions were calculated for $x = 0.4; 0.6; 1.6$;

1.8 compositions. The results are presented in Table 11.

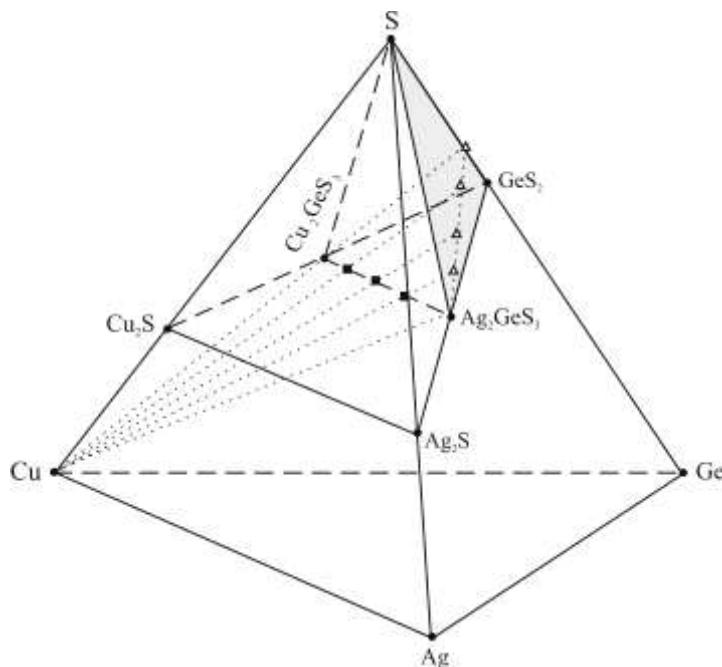


Fig.8. For calculation of integral thermodynamic functions of phases in the Cu_2GeS_3 - Ag_2GeS_3 system

Table 11. Standard integral thermodynamic formation functions and standard entropies of the Cu_2GeS_3 and Ag_2GeS_3 compounds and $(\text{Cu}_2\text{GeS}_3)_x(\text{Ag}_2\text{GeS}_3)_{1-x}$ solid solutions [167]

| Composition | $-\Delta_f G^\circ(298\text{K})$ | $-\Delta_f H^\circ(298\text{K})$ | $S^\circ(298\text{K})$ $\text{J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$ |
|--|----------------------------------|----------------------------------|--|
| | $\text{kJ}\cdot\text{mol}^{-1}$ | | |
| Cu_2GeS_3 | 211.3 ± 2.4 | 213.7 ± 2.3 | 190.3 ± 5.5 |
| $(\text{Cu}_2\text{GeS}_3)_{0.9}(\text{Ag}_2\text{GeS}_3)_{0.1}$ | 212.2 ± 2.1 | 210.7 ± 2.2 | 199.9 ± 5.2 |
| $(\text{Cu}_2\text{GeS}_3)_{0.8}(\text{Ag}_2\text{GeS}_3)_{0.2}$ | 213.3 ± 2.1 | 209.6 ± 2.2 | 209.4 ± 5.7 |
| $(\text{Cu}_2\text{GeS}_3)_{0.7}(\text{Ag}_2\text{GeS}_3)_{0.3}$ | 214.0 ± 2.1 | 208.2 ± 2.2 | 219.1 ± 5.8 |
| $(\text{Cu}_2\text{GeS}_3)_{0.2}(\text{Ag}_2\text{GeS}_3)_{0.8}$ | 208.9 ± 2.1 | 200.7 ± 2.2 | 235.8 ± 8.0 |
| $(\text{Cu}_2\text{GeS}_3)_{0.1}(\text{Ag}_2\text{GeS}_3)_{0.9}$ | 207.4 ± 2.1 | 199.6 ± 2.2 | 238.3 ± 8.3 |
| Ag_2GeS_3 | 206.0 ± 2.1 | 198.0 ± 2.2 | 239.1 ± 8.8 |

5. Copper chalcogenides with arsenic subgroup elements

Cu-As(Sb)-chalcogen systems attract close attention of researchers for two reasons. Firstly, the compounds of these systems and phases based on them are valuable environmentally friendly functional materials with photoelectric, optical [176-192] and thermoelectric [193-202] properties. Secondly, many known ternary compounds of these systems occur in nature in the form of minerals: enargite and lucionite Cu_3AsS_4 ; tennantite

$\text{Cu}_{12}\text{As}_4\text{S}_{31}$, tetrahedrite $\text{Cu}_{12}\text{Sb}_4\text{S}_{31}$; chalcostibite CuSbS_2 ; synnergite $\text{Cu}_6\text{As}_4\text{S}_9$; lautite CuAsS , etc. These mineral compounds are of great interest for mineralogy and geochemistry and provide valuable information about the physical conditions on Earth at the time of their occurrence [36, 37].

Copper-arsenic (antimony) sulfides [176-192] are considered promising candidates for use as *p*-type absorbers in solar cells due to the wide availability and environmental friendliness of the raw material, suitable band gap and high absorption coefficient. The suitable band gap of

these phases indicates the prospect of their application also as wide-bandgap semiconductors in third-generation photovoltaic devices. The largest number [184-191] of works is devoted to chalcostibite CuSbS_2 , which is considered as a substitute material for CuInS_2 due to its similar optical properties and the additional advantage of a higher content of antimony in the Earth and its lower cost compared to indium.

Synthetic analogues of multiple copper minerals [193-198], as well as solutions and composites based on them [198-202] have low thermal conductivity and an anisotropic crystal structure and exhibit promising thermoelectric properties. Thus, in review [198], it was noted that by 2015, zT values of the order of ~ 1.0 at ~ 723 K were achieved for a number of natural and doped tetrahedrite materials, which is comparable to conventional p -type thermoelectric materials. The authors of [202] proposed a new concept for increasing the stability and efficiency of copper thermoelectrics, which consists in producing composites of the "copper chalcogenide-copper tetrahedrite" type. According to these authors, the proposed solution can successfully block excessive migration of copper and stabilize the composition and properties of the material during subsequent thermal cycles.

It should also be noted that, according to a number of studies, copper-bismuth chalcogenides, in particular CuBiS_2 ,

demonstrate good photothermal properties and an anticancer effect [34]. Due to their high X-ray attenuation coefficient, these compounds have the ability to visualize computed tomography [35].

5.1. The Cu-As-X systems

The Cu-As-S system. Numerous works on phase equilibria and properties of ternary phases in the Cu-As-S system covering the period until the early 90s of the last century are summarized in [21, 203]. It is shown that the available data on the Cu_2S - As_2S_3 phase diagram section are contradictory and differ from each other both in the number and composition of ternary compounds, and in the temperatures and nature of their melting. In particular, it was shown in [204] that this system is quasi-binary and is characterized by the formation of ternary compounds Cu_5AsS_4 , Cu_3AsS_3 , $\text{Cu}_{12}\text{As}_4\text{S}_{13}$, $\text{Cu}_4\text{As}_2\text{S}_5$ and $\text{Cu}_6\text{As}_4\text{S}_9$. The authors of [203], taking into a number of studies, presented a slightly different version of the phase diagram from [204], according to which there are 3 ternary compounds in the system: $\text{Cu}_{12}\text{As}_4\text{S}_{13}$, $\text{Cu}_4\text{As}_2\text{S}_5$ and $\text{Cu}_6\text{As}_4\text{S}_9$. It should be noted that the composition of the $\text{Cu}_{12}\text{As}_4\text{S}_{13}$ phase is outside the plane of this section, which casts doubt on the data [203] on its quasi-binarity. [205] presented a new review of the literature on the Cu-As-S system and carried out a critical assessment and thermodynamic modeling of the phase diagram.

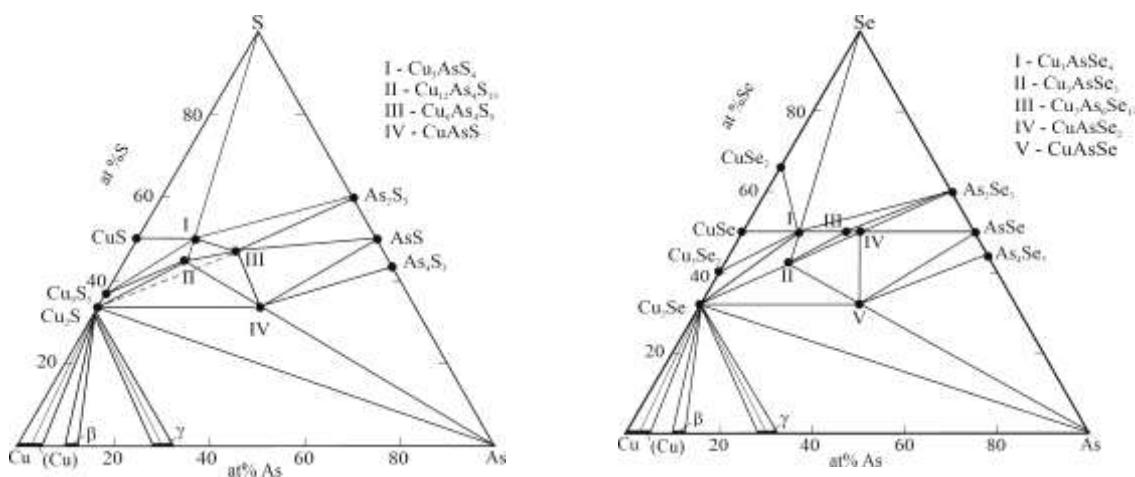


Fig. 9. Diagrams of solid-phase equilibria for the Cu-As-S and Cu-As-Se systems

The studies [206-209] published by our research team the results of a comprehensive

study of phase equilibria and thermodynamic properties of the Cu-As-S system were

presented. The solid-phase equilibrium diagram (Fig. 9) shows ternary Cu_3AsS_4 , $\text{Cu}_{12}\text{As}_4\text{S}_{13}$, $\text{Cu}_6\text{As}_4\text{S}_9$ and CuAsS compounds.

Table 12. Standard thermodynamic functions of formation and standard entropies of the ternary phases of the Cu-As-S(Se) systems

| Compound | $-\Delta_f G^0(298\text{K})$ | $-\Delta_f H^0(298\text{K})$ | $S^0(298\text{K}), \text{J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$ | Ref. |
|--|---------------------------------|------------------------------|--|------------|
| | $\text{kJ}\cdot\text{mol}^{-1}$ | | | |
| Cu_3AsS_4 (enargite) | 179.2±0.6 | 172.2±2.6 | 278±8 | [208, 209] |
| | 211.6 | 215.7 | 276.6 | [216] |
| | 230.4 | 224.0 | 285.0 | [205] |
| | | 179.0 | 256.4 | [37] |
| | | | 277.2 | [217] |
| $\text{Cu}_6\text{As}_4\text{S}_9$ (synnerite) | 445.3±1.6 | 434.6±7.5 | 668±22 | [208, 209] |
| | 517.8 | 505.1 | 673.0 | [205] |
| $\text{Cu}_{12}\text{As}_4\text{S}_{13}$ (tennantite) | 701.8±2.5 | 673.7±10.7 | 1050±13 | [208, 209] |
| CuAsS (lautite) | 69.5±0.3 | 64.1±1.7 | 109±5 | [208, 209] |
| | 76.2 | 76.5 | 100.0 | [205] |
| Cu_3AsSe_4 | 147.3±0.5 | 146.3±1.5 | 307±13 | [213] |
| $\text{Cu}_7\text{As}_6\text{Se}_9$ | 441.8±2.3 | 446.1±11.7 | 970±27 | [59] |
| CuAsSe_2 | 61.1±0.4 | 62.1±1.9 | 149.5±4.5 | [215] |
| | 66.6±0.4 | 67.33±2.0 | 150.9±6.2 | [215] |
| Cu_3AsSe_3 | 141.8±0.5 | 140.0±2.0 | 258.5±5.6 | [59] |
| CuAsSe | 55.1±0.3 | 55.6±2.0 | 109.5±4.7 | [59] |

The Cu-As-Se system. Phase equilibria in this system have been studied in detail along the quasi-binary $\text{Cu}_2\text{Se}-\text{As}_2\text{Se}_3$ section [21, 210, 211]. According to [210], the Cu_3AsSe_3 and CuAsSe_2 compounds are formed in the system. Authors of [211] show the formation of the Cu_3AsSe_3 , $\text{Cu}_4\text{As}_2\text{Se}_5$ and CuAsSe_2 ternary compounds.

The studies [45, 212-215] present the results of studying the phase equilibria and thermodynamic properties of the Cu-As-Se system. It has been established that it is characterized by the presence of ternary compounds Cu_3AsSe_3 , $\text{Cu}_7\text{As}_6\text{Se}_9$, CuAsSe_2 , Cu_3AsSe_4 and CuAsSe (Fig. 9).

The Cu-As-Te system. According to available data [21], no ternary compounds are formed in this system.

Table 12 shows the standard integral thermodynamic functions of copper-arsenic chalcogenides. The data sets obtained by the EDS method [208, 209] for Cu_3AsS_4 , $\text{Cu}_6\text{As}_4\text{S}_9$, and CuAsS are significantly (up to 20%) lower than those given in [205] and are closer to the data in [37, 216]. The standard entropy values

presented in various papers are consistent with each other. Unfortunately, the data [37, 205, 216, 217] are presented without errors, which makes it difficult to assess their reliability. We believe that the data from [205] are greatly overestimated.

5.2. The Cu-Sb-X systems

The Cu-Sb-S system. Research of phase equilibria in the Cu-Sb-S system began at the beginning of the last century. The results of numerous studies in different years were summarized in the monograph [21] and papers [218, 219]. Phase equilibria of the Cu-S-Sb system are calculated in the recently published work [220] utilizing the CALPHAD (CALculation of PHase Diagrams) technique and a new version of the T-diagram of the $\text{Cu}_2\text{S}-\text{Sb}_2\text{S}_3$ section was presented. This diagram significantly different from previous reports.

The complete T-x-y diagram and various sections of the phase diagram, including the isothermal section at 300 K (Fig. 10), are presented by us in [221, 222]. According to their data, the system contains ternary compounds Cu_3SbS_4 , $\text{Cu}_{12}\text{Sb}_4\text{S}_{13}$, $\text{Cu}_{14}\text{Sb}_4\text{S}_{13}$,

Cu_3SbS_3 and CuSbS_2 , in addition, the $\text{Cu}_2\text{S}-\text{Sb}_2\text{S}_3$ cut, in contrast to the literature data, is non-quasi-binary.

Table 13. Standard thermodynamic functions of formation and standard entropy of some ternary copper–antimony (bismut) chalcogenides

| Compound | $-\Delta_f G^0(298\text{K})$ | $-\Delta_f H^0(298\text{K})$ | $S^0(298\text{K}), \text{J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$ | Ref. |
|--|---------------------------------|------------------------------|--|-------|
| | $\text{kJ}\cdot\text{mol}^{-1}$ | | | |
| Cu_3SbS_4 | 254.7 ± 2.3 | 247.8 ± 2.3 | 295.6 ± 7.0 | [221] |
| CuSbS_2 | 128.5 ± 2.2 | 126.9 ± 2.4 | 147.5 ± 3.8 | [221] |
| | $*132.7 \pm 4.2$ | 130.8 ± 4.4 | - | [223] |
| | 130.6 ± 6.0 | 131.7 ± 5.2 | - | [224] |
| $\text{Cu}_{12}\text{Sb}_4\text{S}_{13}$ | 958.7 ± 9.6 | 929.7 ± 11.2 | 1092.0 ± 29.0 | [221] |
| Cu_3SbS_3 | 226.4 ± 2.3 | 219.0 ± 2.6 | 265.5 ± 7.2 | [221] |
| | $*221.6 \pm 6.0$ | 215.0 ± 6.2 | - | [223] |
| $\text{Cu}_{14}\text{Sb}_4\text{S}_{13}$ | 971.7 ± 9.8 | 984.8 ± 11.9 | 1018.0 ± 33.0 | [221] |
| Cu_3SbSe_4 | 191.6 ± 2.5 | 178.6 ± 5.4 | 358.18 | [59] |
| CuSbSe_2 | 101.4 ± 1.8 | 98.5 ± 2.2 | 173 ± 8 | [59] |
| | 77.3 ± 1.3 | 104.8 ± 1.7 | - | [224] |
| Cu_3SbSe_3 | 175.6 ± 2.5 | 164.0 ± 5.3 | 311 ± 15 | [59] |
| CuBiS_2 | 138.6 ± 4.0 | 138.2 ± 2.9 | 156 ± 12 | [45] |
| Cu_3BiS_3 | 213.0 ± 4.4 | 209.9 ± 5.2 | 264 ± 21 | [45] |
| CuBi_3S_5 | 248.7 ± 1.9 | 248.6 ± 5.8 | 421.9 ± 7.8 | [45] |
| CuBiSe_2 | 107.6 ± 0.8 | 105.9 ± 2.51 | 189.8 ± 2.4 | [225] |
| Cu_3BiSe_3 | 162.5 ± 1.2 | 155.9 ± 5.7 | 315.0 ± 8.5 | [225] |
| Cu_9BiSe_6 | 324.8 ± 3.5 | 313.1 ± 18.6 | 659 ± 28 | [225] |

Note: * - our calculation from calorimetric data [223].

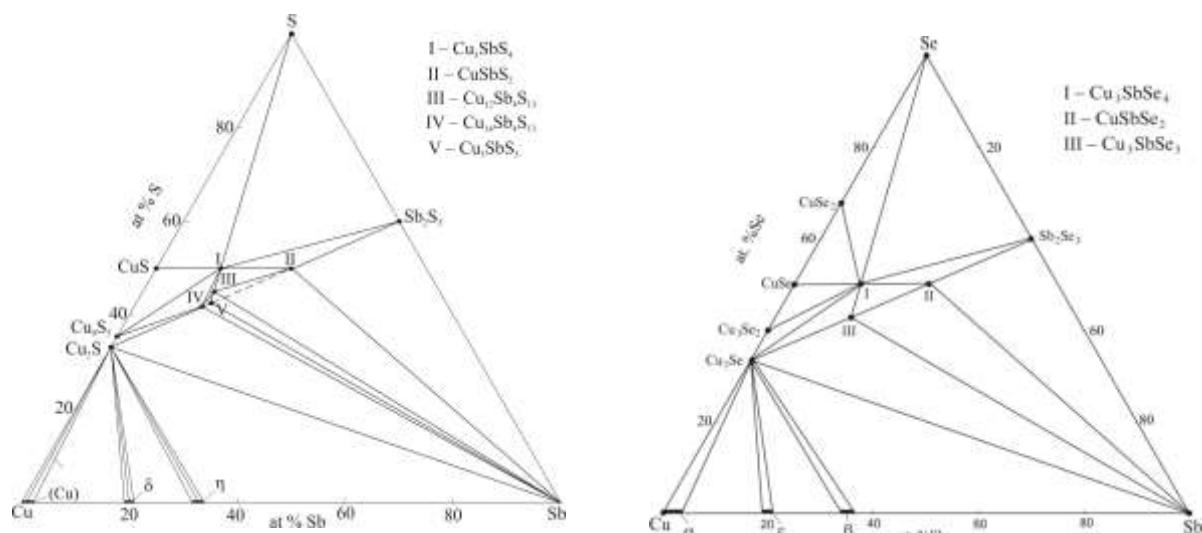


Fig. 10. Diagrams of solid-phase equilibria of the Cu-Sb-S and Cu-Sb-Se systems

The **Cu-Sb-Se system** is characterized by the formation of ternary compounds Cu_3SbSe_4 , CuSbSe_2 and Cu_3SbSe_3 [21] (Fig. 10). The first two compounds melt congruently, and the third one melts incongruently via a peritectic

reaction.

The **Cu-Sb-Te system**. According to available data [21], no ternary compounds are formed in this system. The compound CuSbTe_2 indicated in some early studies was not

subsequently confirmed.

5.3. The Cu-Bi-X systems

The Cu-Bi-S system. Phase equilibria in this system have been studied in numerous studies over more than 100 years. A review of

the available data is given in [21, 219]. According to the solid-phase equilibrium diagram, the following copper-bismuth sulfides exist at room temperature: CuBi₃S₅, CuBiS₂ and Cu₃BiS₃ (Fig. 11).

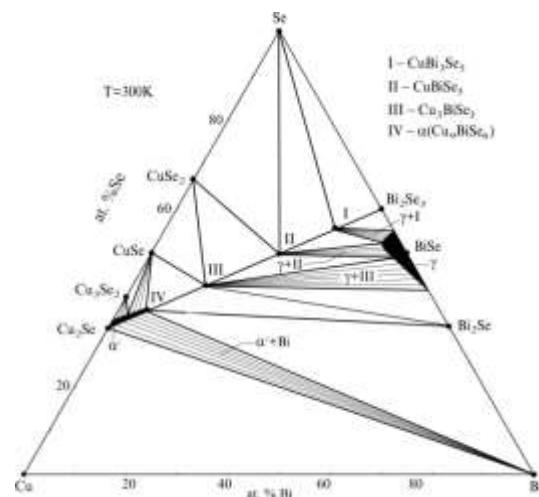
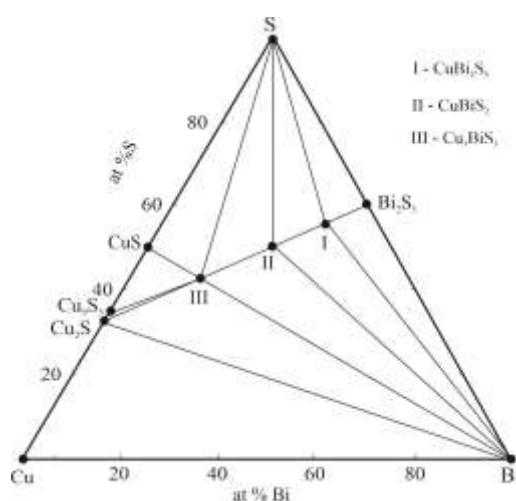


Fig. 11. Solid-phase equilibrium diagrams of Cu-Bi-S(Se) systems

The Cu-Bi-Se system. The paper [225] summarizes the results of all available studies on phase equilibria and presents a complete picture of phase equilibria, including the liquidus surface, a series of polythermal sections and an isothermal section at room temperature of the phase diagram (Fig. 11). In this system, as in the sulfur-containing system, three ternary compounds CuBi₃Se₅, CuBiSe₂ and Cu₃BiSe₃ were identified. These compounds melt incongruently.

The Cu-Bi-Te system. According to available data [21], no ternary compounds are formed in this system.

Table 13 shows data on the standard integral thermodynamic functions of copper-antimony and medibismuth chalcogenides. For almost all of these compounds, complete sets of thermodynamic quantities were obtained using the EMF method with a Cu⁺ conducting electrolyte. The thermodynamic functions of CuBi₃Se₅, CuBiSe₂ and Cu₃BiSe₃, determined by the EDS method [59, 221] (exception for the $-\Delta_f G^0(298K)$ of the last compound) are in good agreement with calorimetric data [223, 224].

Conclusion

This work summarizes the results of studies, including ours, on the thermodynamic properties of copper chalcogenides with heavy p¹-p³ elements. It is shown that, there are mutually consistent sets of data on solid-phase equilibria and fundamental thermodynamic functions for copper chalcogenides with thallium and with elements of the germanium and arsenic subgroups. It is also noted that most of the existing works were carried out using various modifications of the equilibrium method of chemical thermodynamics - the EMF method.

Considering the exceptional importance of phase diagrams in studies by this method, in addition to thermodynamic data, this work also presents data on solid-phase equilibria of the corresponding systems.

Our analysis also showed that the thermodynamic properties of copper chalcogenides with gallium, indium and silicon have been practically not studied, and the available data are contradictory.

In conclusion, we note that the capabilities of the thermodynamic approach are not fully

used in the development of complex functional materials, in particular copper-based chalcogenides; the empirical approach often prevails. We consider it important to develop

thermodynamic research and wide application of their results in the design of new complex chalcogenide materials.

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MİSİN MÜRƏKKƏB XALKOGENİDLƏRİNİN TERMODİNAMİK XASSƏLƏRİ

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Misin mürəkkəb xalkogenidləri maraqlı termoelektrik, fotoelektrik, optik, ion keçiriciliyi və digər xassələrə malik olan ən mühüm ekoloji təhlükəsiz funksional materiallar hesab edilirlər. Coxsayılı tədqiqatların təhlili göstərir ki, bu birləşmələrin tətbiq xüsusiyyətlərinin yaxşılaşdırılması struktur və tərkibin manipulyasiyası ilə əlagəlidir. Belə proseslərin optimallaşdırılmasının effektiv həlli onların dərin termodinamik analizini tələb edir ki, bu da öz növbəsində müvafiq maddələrin fundamental termodinamik xassələri haqqında etibarlı məlumatların olmasına labüd edir. İcmalda misin bəzi p¹-p³ elementləri ilə xalkogenidlərinin termodinamik xassələri üzrə tədqiqatların, o cümlədən müəlliflərin öz işlərinin nəticələri ümumiləşdirilmişdir. Ədəbiyyat analizi göstərdi ki, bu işlərin böyük əksəriyyəti elektrik hərəkət qüvvəsi (EHQ) metodunun müxtəlif modifikasiyalarından istifadə etməklə həyata keçirilib. Kimyəvi termodinamikanın bu tarazlıq üsulu ilə aparılan təcrübələrin planlaşdırılması və onların məlumatlarının emalı etibarlı faza tarazlığı mənzərəsi olmadan mümkün deyil. Bunu nəzərə alaraq, işdə termodinamik məlumatlarla yanaşı, EHQ üsulu ilə tədqiq olunan bir sıra sistemlərin bərk faza tarazlıqlarının diaqramları da təqdim edilmişdir.

Ədəbiyyat təhlili göstərdi ki, Cu-Tl-X, Cu-Ge(Sn)-X (X-S, Se, Te) və Cu-As(Sb, Bi)-S(Se) sistemlərində faza tarazlıqları və üçlü birləşmələrin termodinamik xassələri haqqında qarşılıqlı tənzimlənmiş məlumatlar mövcuddur. Cu-Tl-X və Cu-Sn-Se sistemlərin üçlü birləşmələrinin termodinamik funksiyaları EHQ metodunun iki modifikasiyası, yəni iki müxtəlif komponentin misin və ya talliumun (qalayın) parsial molyar funksiyalarının təyin etməklə müəyyən edilmişdir. Misin gallium, indium və silisium ilə xalkogenidlərinin termodinamik xassələri praktiki olaraq öyrənilməmişdir, mövcud olan məlumatlar isə ziddiyyətlidir.

Açar sözlər: misin mürəkkəb xalkogenidləri, ekoloji təhlükəsiz materiallar, mis əsasında üçlü sistemlər, faza diaqramları, termodinamik xassələr, EHQ üsulu.

ТЕРМОДИНАМИЧЕСКИЕ СВОЙСТВА СЛОЖНЫХ ХАЛЬКОГЕНИДОВ МЕДИ

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Сложные халькогениды на основе меди относятся к важнейшим экологически безопасным функциональным материалам, имеющим большой потенциал применения, благодаря интересным термоэлектрическим, фотоэлектрическим, оптическим и др. свойствам, а также ионной проводимостью. Анализ данных многочисленных исследований показывает, что улучшение прикладных характеристик этих соединений связано с манипуляцией структуры и состава. Эффективное решение вопросов оптимизации таких процессов требует их глубокого термодинамического анализа, для которого необходимы надежные данные по фундаментальным термодинамическим характеристикам соответствующих веществ. В данном обзоре обобщены результаты работ, в том числе авторов, по термодинамическим свойствам халькогенидов меди с некоторыми p¹-p³ элементами. Анализ показал, что подавляющее большинство этих работ выполнено

различными модификациями метода электродвижущих сил (ЭДС). Планирование экспериментов проводимых этим равновесным методом химической термодинамики и обработка их данных невозможна без наличия надежных по фазовым равновесиям. Учитывая это в работе помимо термодинамических данных приведены также диаграммы твердофазных равновесий ряда систем, изученных методом ЭДС.

Анализ показал, что для тройных систем Cu-Tl-X, Cu-Ge(Sn)-X (X-S, Se, Te) и Cu-As(Sb, Bi)-S(Se) имеются взаимосогласованные данные по фазовым равновесиям и термодинамическим функциям тройных соединений, причем для систем Cu-Tl-X и Cu-Sn-Se термодинамические функции тройных соединений определены двумя модификациями метода ЭДС путем определения парциальных молярных функций двух различных компонентов – меди и таллия(олова). В тоже время термодинамические свойства халькогенидов меди с галлием, индием и кремнием практически не изучены, а имеющиеся данные противоречивы.

Ключевые слова: сложные халькогениды меди, экологически безопасные материалы, тройные медьсодержащие системы, фазовые диаграммы, термодинамические свойства, метод ЭДС.